# Controlling evaporation of liquid $\mathrm{CO}_{2}$ during transport as part of CCS 

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#### Abstract

: In Europe, deployment of large-scale carbon capture and storage (CCS) with storage in an underground geological formation will in practice imply off-shore storage. This implies separation, purification and liquefaction of $\mathrm{CO}_{2}$ and, after transport to a harbour facility, loading into a ship for transport to the storage site, a trip that may take several days. The topic of this paper is how to address the evaporation of some of the liquefied $\mathrm{CO}_{2}$ caused by heat leaking into the storage, resulting in rising pressure and temperature that should be controlled. First, this paper will assess the dependence of liquefied $\mathrm{CO}_{2}$ evaporation with time (boil-off rate, BOR) on starting (low, medium or high) pressures/temperatures and heat ingress, and the rate of pressure and temperature increase as a result of it. Secondly, it will suggest alternatives to re-liquefaction during the transport. The latter could involve, for example, the use of zeolite or other sorbent, or adding small amounts of a component with slightly different thermodynamic properties to the $\mathrm{CO}_{2}$. As the first part of the paper shows, based on the behaviour of pure $\mathrm{CO}_{2}$ there may not be a need for worries or action since the pressure rise is very modest even after several days. The work also shows that small amounts of impurities may have significant effects, emphasising the importance of pre-transport processing.


## Keywords:

Carbon dioxide capture and storage (CCS), transport, liquefied $\mathrm{CO}_{2}$, evaporation, refrigeration.

## 1. Introduction

In Europe, deployment of large-scale carbon capture and storage (CCS) with storage in an underground geological formation will in practice imply off-shore storage. Off the coast of Norway this has been practiced already since the mid-1990s at the Sleipner and (later) Snøhvit sites where ~ $1 \mathrm{Mt} / \mathrm{yr}$ and $\sim 0.7 \mathrm{Mt} / \mathrm{yr}$, respectively, $\mathrm{CO}_{2}$ are separated from produced natural gas and stored under the seabed [1]. Current developments aim at expanding Norway's CCS to $\mathrm{CO}_{2}$ from the Klemetsrud waste incinerator of Fortum Oslo Värme and Norcem's cement production facility at Brevik, for ~ $0.4 \mathrm{Mt} / \mathrm{yr}$ each. If during winter 2020/2021 Norwegian parliament makes a positive financing decision, commercial operation will start during 2023/2024, involving separation, purification and liquefaction of $\mathrm{CO}_{2}$ and, after transport to a harbour facility, loading into a ship for transport to the storage site, a trip that may take several days.
Transport of $\mathrm{CO}_{2}$ as part of CCS activities can involve transport of compressed gaseous or liquefied $\mathrm{CO}_{2}$. Trucks, trains or ship can be used depending primarily on transport distance, amount and frequency of that amount [2]. One issue that needs to be considered for transport of liquefied $\mathrm{CO}_{2}$ is the evaporation of some of the load as a result of heat leaking in from the surroundings, causing a rise in pressure that may become problematic. A recent study [3] considered re-liquefaction of boil-off gas from liquefied $\mathrm{CO}_{2}$ transport on board a ship to be necessary and presents several process layouts for the implementation of an on-board refrigeration system.
This study aims at assessing the need for re-liquefaction for transport of liquefied $\mathrm{CO}_{2}$ at a starting pressure of 15 bar (boiling point $-28.1^{\circ} \mathrm{C}$ ) rather than 7 bar (boiling point $-49.3^{\circ} \mathrm{C}$ ) as considered in [3], followed by suggestions for how to act rather than re-liquefy the boil-off gas (BOG). Obviously, although depending to some extent on the off-loading process set-up at the $\mathrm{CO}_{2}$ underground storage site, a large amount of BOG may result in a large amount of gaseous $\mathrm{CO}_{2}$ that needs to be transported back to its source for re-liquefaction.

## 2. Analysis of liquid $\mathrm{CO}_{2}$ evaporation

### 2.1. Pressure and temperature rise as a result of heat ingress

This first assessment considers pure $\mathrm{CO}_{2}$, neglecting the effect of minor amounts of contaminants. A heat ingress $\mathrm{Q}(\mathrm{J})$ into a constant volume of liquefied $\mathrm{CO}_{2}$ with some overhead vapour (gas) will increase the enthalpy of the two-phase system. This will give a pressure change as well as a change in temperature, restricted by the constant total volume of liquid and gas combined $\mathrm{V}_{\text {total }}$, and of course constant total mass $\mathrm{m}_{\text {total }}$. Thus, since the constant total volume prevents work W done on or by the system, the First Law of Thermodynamics for internal energy $U$ is simplified:

$$
\begin{equation*}
\Delta U=Q+W \quad \rightarrow \Delta U=Q \tag{1}
\end{equation*}
$$

Dividing the system in a vapour (gas) phase and a liquid phase with changing amounts gives work by the increasing amount of gas on the liquid phase being balanced by work experienced by the liquid phase: $\int \mathrm{p} \cdot \mathrm{dV} \mathrm{V}_{\mathrm{L}}=-\int \mathrm{p} \cdot d V_{\mathrm{G}}$, or $\Delta \mathrm{p} V_{\mathrm{L}}+\Delta \mathrm{p} V_{\mathrm{G}}=0$ for the constant volume system. Then,

$$
\begin{equation*}
Q=\Delta U=\Delta U_{L}+\Delta U_{G}=\Delta U_{L}+\Delta U_{G}+\Delta p V_{L}+\Delta p V_{G}=\Delta H_{L}+\Delta H_{G}=\Delta H \quad \text { (J) } \tag{2}
\end{equation*}
$$

Describing the state of the $\mathrm{CO}_{2}$ by its enthalpy as function of temperature T and pressure p , i.e. $\mathrm{h}(\mathrm{T}, \mathrm{p})$ $(\mathrm{kJ} / \mathrm{kg})$ gives, for the two-phase system at its boiling point, one degree of freedom according to Gibbs' phase rule. This allows for vapour mass fraction, x , defining the liquid-vapour mixture enthalpy.
For transport of $\mathrm{CO}_{2}$ with a given boil-off rate (BOR) the increase of x is defined which makes it more convenient to use $\mathrm{h}(\mathrm{x}, \mathrm{p})$ in the energy equations. This fixes the saturation temperature (the boiling point) as function of the changing pressure. Thus:

$$
\begin{equation*}
h=h(x, p)=x \cdot h_{G}+(1-x) \cdot h_{L} \tag{3}
\end{equation*}
$$

which for pressure changes gives

$$
\begin{align*}
\frac{d h}{d p}=\left(\frac{\partial h}{\partial x}\right)_{p} \cdot \frac{d x}{d p}+ & \left(\frac{\partial h}{\partial p}\right)_{x}=h_{G} \cdot \frac{d x}{d p}+h_{L} \cdot \frac{d(1-x)}{d p}+x \cdot \frac{d h_{G}}{d p}+(1-x) \cdot \frac{d h_{L}}{d p} \\
& =\frac{d x}{d p} \cdot\left(h_{G}-h_{L}\right)+x \cdot \frac{d h_{G}}{d p}+(1-x) \cdot \frac{d h_{L}}{d p} \tag{4}
\end{align*}
$$

Appendix A gives data for $\mathrm{CO}_{2}$, giving values as polynomials for enthalpy $h_{G, \text { sat }}$ and $h_{L, \text { sat }}$ (Eqs. A.5A.7) at the saturation state that give simple relations for $d h_{G} / d p$ and $d h_{L} / d p$ at the saturation state, all as function of pressure $\mathrm{p}\left(=\mathrm{p}_{\text {sat }}\right)$.
Using (4), the pressure variation with time $\Delta \mathrm{p} / \Delta \mathrm{t}$ can be derived if the heat ingress $Q=\dot{Q} \cdot \Delta t$ during time interval $\Delta t$ is known:

$$
\begin{align*}
\dot{Q}=\frac{\Delta H}{\Delta t}=\frac{m_{t o t} \cdot \Delta h}{\Delta p} \cdot \frac{\Delta p}{\Delta t}= & m_{t o t} \cdot\left(\frac{\Delta x}{\Delta p} \cdot\left(h_{G}-h_{L}\right)+x \cdot \frac{d h_{G}}{d p}+(1-x) \cdot \frac{d h_{L}}{d p}\right) \cdot \frac{\Delta p}{\Delta t}  \tag{5}\\
& \rightarrow \frac{\Delta p}{\Delta t}=\frac{\dot{Q} / m_{t o t}}{\frac{\Delta x}{\Delta p} \cdot\left(h_{G}-h_{L}\right)+x \cdot \frac{d h_{G}}{d p}+(1-x) \cdot \frac{d h_{L}}{d p}} \tag{6}
\end{align*}
$$

The term $\Delta \mathrm{x} / \Delta \mathrm{p}$ can be determined from a mass balance combined with total volume balance, density as function of pressure relations, information on the boil-off rate (BOR) and the starting value for x . Since total volume and total mass are both constant this gives:

$$
\begin{gather*}
V_{\text {total }}=V_{G}+V_{L}=\frac{m_{G}}{\rho_{G}}+\frac{m_{L}}{\rho_{L}}  \tag{7}\\
\frac{V_{\text {total }}}{m_{\text {total }}}=\text { constant }=\frac{x}{\rho_{G}}+\frac{1-x}{\rho_{L}}=\frac{x}{\rho_{G}(p)}+\frac{1-x}{\rho_{L}(p)} \rightarrow x=\frac{\text { constant } \cdot \rho_{L}-1}{\frac{\rho_{L}}{\rho_{G}}-1} \tag{8}
\end{gather*}
$$

at all times, with expressions for saturation state densities $\rho_{\mathrm{G}, \text { sat }}$ and $\rho_{\mathrm{L}, \text { sat }}$ as function of (saturation) pressure given in Appendix A, Eqs. A.2-A.4. Thus, x is directly related to pressure from which the above mentioned $\Delta x / \Delta \mathrm{p}$ for Eq. (6) and the (saturation) temperature can be calculated.

## 2.2. $\mathrm{CO}_{2}$ evaporation during five days liquid $\mathrm{CO}_{2}$ transport

With the thermodynamics given above, the dynamics of the evaporation of some of the liquefied $\mathrm{CO}_{2}$ can be calculated which is here done for a five-day travel shipload of $7500 \mathrm{~m}^{3}$ liquefied $\mathrm{CO}_{2}$, with $99 \%$ liquid volume, starting with 15 bar pressure $\left(\mathrm{CO}_{2}\right.$ boiling point $\left.-28.1^{\circ} \mathrm{C}\right)$. This implies 7960491 kg liquid $\mathrm{CO}_{2}$ and 2942 kg gaseous $\mathrm{CO}_{2}$, giving $\mathrm{x}=3.69 \times 10^{-4}$, and a (constant) total specific volume $\mathrm{V}_{\text {total }} / \mathrm{m}_{\text {total }}=9.42 \times 10^{-4} \mathrm{~m}^{3} / \mathrm{kg}$. (Note that in [3], three to four days sailing is considered "short".)
As input data, an evaporation rate of $0.1 \%$ of the liquid $\mathrm{CO}_{2}$ per day is assumed, within the $0.05-$ $0.15 \% /$ day range typical for LNG transport [4]. This implies that each hour a fraction $0.1 \times 10^{-2} / 24$ $((\mathrm{kg} / \mathrm{kg}) / \mathrm{h})$ of the liquid volume but also of the liquid mass goes from the liquid phase to the gas phase. With this, the changing mass of gas and its mass fraction x as function of time can be quantified for time step $\Delta \mathrm{t}=1 \mathrm{~h}$ (where $\Delta \mathrm{x} / \Delta \mathrm{t}$ equals $\mathrm{x}^{\mathrm{i}+1}-\mathrm{x}^{\mathrm{i}}$ :

$$
\begin{gather*}
m_{G}^{i+1}=m_{G}^{i}+\left(m_{t o t}-m_{G}^{i}\right) \cdot \frac{0.001}{24}  \tag{9}\\
x^{i+1}=\frac{m_{G}^{i+1}}{m_{t o t}}=\frac{m_{G}^{i}+\left(m_{t o t}-m_{G}^{i}\right) \cdot \frac{0.001}{24}}{m_{t o t}}=x^{i}+\left(1-x^{i}\right) \cdot \frac{0.001}{24} \tag{10}
\end{gather*}
$$



Fig. 1 Increasing pressure and temperature (left) and amount of $\mathrm{CO}_{2}$ vapour (right) versus time during a five-day transport for the reference case (15 bar and $1 \%$ volume as gas at the start, BOR $0.1 \% / d a y$ )

For these system dynamics the variation of pressure, gas mass and mass fraction $\mathrm{CO}_{2}$ and temperature can be calculated, with results as in Figs. 1. Clearly, a dramatic rise in pressure is hardly to be expected even during a five-day transport while also the temperature rises only with $0.8^{\circ} \mathrm{C}$. Gas max fraction x increases from $<0.04 \%$ to $<0.5 \%$ (mass). One may question whether any special measures are needed when this occurs.

## 2.3. $\mathrm{CO}_{2}$ evaporation parameter sensitivity

While the results in Fig. 1 do not seem to call for special measures like collection and re-liquefaction of the BOG, a sensitivity analysis may shed light on how starting conditions and process system parameters affect the behaviour of the liquefied $\mathrm{CO}_{2}$.
Fig. 2 shows the outcome for a lower starting pressure of 10 bar, which would require refrigeration to $-40.6^{\circ} \mathrm{C}$. With a $0.1 \% /$ day BOR and $1 \%$ of the transport volume filled with gaseous $\mathrm{CO}_{2}$ above the liquefied $\mathrm{CO}_{2}$ again a pressure rise $<0.5$ bar is seen after 5 days with a temperature rise of $1.3^{\circ} \mathrm{C}$. The increase of gas mass and gas mass fraction x are not changed compared to the reference case.


Fig. 2 Increasing pressure and temperature (left) and amount of $\mathrm{CO}_{2}$ vapour (right) versus time during a five-day transport for a lower pressure case (10 bar and 1\% volume as gas at the start, BOR $0.1 \% / d a y)$

The same modest differences are found for a higher starting pressure of 20 bar which would require refrigeration to $-19.3^{\circ} \mathrm{C}$ : a pressure rise $<0.4$ bar and a temperature rise $<0.5^{\circ} \mathrm{C}$, as shown in Fig. 3 . A lower temperature obviously gives a larger driving force for heat ingress, which is approx. 13.3 W per kg transported $\mathrm{CO}_{2}$, comparable to 12.5 W for the reference case (Fig. 1) and 11.7 W for the previous case (Fig.2). Also for this third case the increase of gas mass and gas mass fraction x are not changed.
As may be expected, a more dramatic effect follows from a higher BOR: Fig. 4 shows the results obtained with a doubled, relatively high [4] BOR of $0.2 \%$ per day. This corresponds to a heat ingress of 25 W per kg transported $\mathrm{CO}_{2}$. Final mass of gas is almost doubled while the final gas mass fraction x is $>0.1$, as shown in Fig. 4. Pressure rise is 1.4 bar while the temperature rise is doubled to $1.5^{\circ} \mathrm{C}$ from $0.8^{\circ} \mathrm{C}$ for the reference case.


Fig. 3 Increasing pressure and temperature (left) and amount of $\mathrm{CO}_{2}$ vapour (right) versus time during a five-day transport for a higher pressure case (20 bar and $1 \%$ volume as gas at the start, BOR 0.1 \%/day)


Fig. 4 Increasing pressure and temperature (left) and amount of $\mathrm{CO}_{2}$ vapour (right) versus time during a five-day transport for a higher BOR case ( 15 bar and $1 \%$ volume as gas at the start, BOR $0.2 \% / d a y$ )

The final case simulated was a larger amount of initial volume filled with gas above the liquefied $\mathrm{CO}_{2}$ when starting the transport, being $3 \%$ of the storage volume rather than $1 \%$. While this does have some effect on the amount of gas transported versus time and its mass fraction there is hardly a difference from the reference case when it comes to pressure and temperature rise, as shown in Fig. 5. The heat ingress is also practically the same at around 12.5 W per kg transported $\mathrm{CO}_{2}$.

Altogether, it can be concluded that for transport of pure $\mathrm{CO}_{2}$ in liquid form, neglecting the effect of contaminants, hardly a problematic rise in temperature or pressure would arise for a BOR of $1 \%$ per day. It does not agree with "the tank will explode unless the BOG is removed or reliquefied. Thus, treatment of the $B O G$ is a must to consider in designing a $\mathrm{CO}_{2}$ transport ship." as stated in [3].


Fig. 5 Increasing pressure and temperature (left) and amount of $\mathrm{CO}_{2}$ vapour (right) versus time during a five-day transport for a higher gas phase starting volume case ( 15 bar and $3 \%$ volume as gas at the start, BOR 0.1 \%/day)

## 3. Suggestions for controlling pressure and temperature rise

Somewhat surprisingly, the analysis given above for a shipment of pure liquefied $\mathrm{CO}_{2}$ does not show a significant or dramatic rise of pressure or temperature. The above reference case with $0.1 \% /$ day BOR gives $\sim 330 \mathrm{~kg} / \mathrm{h}$ gas production. The work in [3,5] considers $1000 \mathrm{~kg} / \mathrm{h}$ BOG processing from $0.05 \% /$ day BOR from a $50000 \mathrm{~m}^{3}$ storage capacity vessel (much larger than the $7500 \mathrm{~m}^{3}$ considered above), evaporating at 7 bar (where the boiling point for $\mathrm{CO}_{2}$ is $-51.5^{\circ} \mathrm{C}$ ), while transporting $99.5 \% / 0.5 \% \mathrm{vol} / \mathrm{vol} \mathrm{CO}_{2} / \mathrm{N}_{2}$ liquid. That gave a $64 \% / 36 \% \mathrm{vol} / \mathrm{vol} \mathrm{CO}_{2} / \mathrm{N}_{2}$ boil-off gas, as a result of a much higher relative volatility for $\mathrm{N}_{2}$. Unfortunately [3,5] do not report neither a pressure or temperature rise nor the rate of these.
As shown above, a lower $\mathrm{CO}_{2}$ transport temperature gives a larger heat ingress simply as a result of a larger temperature difference driving force. Moreover, a higher transport pressure would require a stronger (thicker walls) $\mathrm{CO}_{2}$ storage which probably gives better heat insulation as well (although a higher pressure does give a somewhat lower density for the liquefied $\mathrm{CO}_{2}$, increasing the necessary volume.) Thus, it seems that BOR can be reduced by operating at higher pressures rather than low temperatures, also from an energy efficiency point of view if the energy penalty of re-liquefaction can be avoided.
The presence of contaminants has a significant influence on the composition of the BOG as the work in [3] shows. Nitrogen has a lower heat of evaporation and a much lower boiling point than $\mathrm{CO}_{2}$ for a given pressure, and a lower liquid density as well. It would preferably occur near the liquid - vapour interface and show a higher rate of evaporation than $\mathrm{CO}_{2}$. The gas phase will nonetheless contain a large $\mathrm{CO}_{2}$ fraction and simply purging the BOG is not an option. Similarly, increasing the fraction of nitrogen in the liquefied $\mathrm{CO}_{2}$ until a, say, $>95 \%$ nitrogen BOG is obtained is not an option.
Besides nitrogen, contaminants that are more volatile than $\mathrm{CO}_{2}$ are methane, hydrogen, argon and carbon monoxide. These are flammable or (argon) inert and some methane (as LNG) or ethane (with a boiling point similar to $\mathrm{CO}_{2}$ ) may be added to the transported liquefied $\mathrm{CO}_{2}$ so that a flammable BOG mixture is obtained for the engines that drive the ship (or transport vehicle in general). See [6] for low-temperature $\mathrm{CO}_{2}-\mathrm{N}_{2}, \mathrm{CO}_{2}-\mathrm{CH}_{4}, \mathrm{CO}_{2}-\mathrm{C}_{2} \mathrm{H}_{6}$ and several other CCS-relevant phase diagrams (and a discussion on the importance of mixing enthalpy).
Alternatively, adsorption of $\mathrm{BOG} \mathrm{CO}_{2}$ on molecular sieves or active carbon can be considered: when pressure is reduced during off-loading of $\mathrm{CO}_{2}$ at the point of underground storage the adsorbed $\mathrm{CO}_{2}$ would be released and become available for storage as well. If ammonia, $\mathrm{NH}_{3}$ is available at an
attractive cost an gaseous overhead space of ammonia above the liquefied $\mathrm{CO}_{2}$ may give production of ammonium (bi)carbonate (ABC, AC) similar to the chilled ammonia process (CAP) for removal of $\mathrm{CO}_{2}$ from flue gas at $\sim 5^{\circ} \mathrm{C}$ [7]. Formation of AC and/or ABC powder will effectively suppress a rising pressure. Again, these solid salts will decompose during a pressure reduction in the storage tank upon off-loading for storage.
Most of the above deserves further analysis, for example experimentally (e.g [8]). At this point no urgency seems to exist if not very long (more than a week) duration CCS travel with liquefied $\mathrm{CO}_{2}$ is planned. If impurities in the liquefied $\mathrm{CO}_{2}$ become a critical or expensive factor during transport then a better on-shore pre-processing before transport is the most cost-effective solution. Goos et al. recommend no free water and limited concentrations of contaminants and non-condensable gases [9].

## 4. Conclusions

For a better understanding pressure and temperature rise during transport of liquefied $\mathrm{CO}_{2}$ as part of a CCS process train, the thermodynamics of a liquid/vapour pure $\mathrm{CO}_{2}$ system is analysed. Based on this it can be concluded that for pure $\mathrm{CO}_{2}$ a significant rise in pressure and temperature is not to be expected when starting of at $15 \operatorname{bar}\left(-28^{\circ} \mathrm{C}\right)$ and a boil-off rate (BOR) of $0.1 \% /$ day. Comparison with (scarce) literature suggests that these conditions are preferable over 7 bar $\left(-49^{\circ} \mathrm{C}\right)$ conditions to start with, as a larger temperature difference with the surroundings apparently increase the BOG rate. The role of impurities that have a higher volatility than $\mathrm{CO}_{2}$ warrants more study. For example, adsorbents like zeolite or active carbon may adsorb $\mathrm{BOG} \mathrm{CO}_{2}$, and so can ammonia form solid (bi)carbonate: these sorbents or salts would re-release the $\mathrm{CO}_{2}$ during a pressure reduction at $\mathrm{CO}_{2}$ off-loading. If impurities in the liquefied $\mathrm{CO}_{2}$ become a critical factor during transport then a better (on-shore) preprocessing is recommended.

## Appendix A - Thermodynamic data $\mathbf{C O}_{2}$

For this paper, thermodynamic data for $\mathrm{CO}_{2}$ as a two-phase system of saturated liquid and saturated vapour is considered for the pressure range $10-25$ bar (abs). This corresponds to $-40--16^{\circ} \mathrm{C}$. A $\log$ pressure - enthalpy diagram for $\mathrm{CO}_{2}$ as can be found on-line [10] is given below; for the calculations using data on the saturated states an on-line calculator [11] was used that gave data as collected in Table A.1.

Table A.1. Data for saturated $\mathrm{CO}_{2}$ liquid and vapour

| Pressure, <br> bar abs | $\mathrm{T}_{\text {sat }}$, | $\rho_{\mathrm{L}, \text { sat }} \mathrm{C}$ <br> $\mathrm{kg} / \mathrm{m}^{3}$ | $\rho_{\mathrm{G}, \text { sat }}$ <br> $\mathrm{kg} / \mathrm{m}^{3}$ | $\rho_{\mathrm{L}_{\text {sat }} /} /$ <br> $\rho_{\mathrm{G}, \text { sat },}-$ | $\mathrm{h}_{\mathrm{L}, \text { sat }}$ <br> $\mathrm{kJ} / \mathrm{kg}$ | $\mathrm{h}_{\mathrm{G}, \text { sat }} \mathrm{k}$ <br> $\mathrm{J} / \mathrm{kg}$ | $\mathrm{h}_{\mathrm{G}, \text { sat }}-\mathrm{h}_{\mathrm{L}, \text { sat }}$ <br> $\mathrm{kJ} / \mathrm{kg}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 10 | -40.14 | 1116.55 | 25.99 | 42.96 | 112.62 | 435.27 | 322.65 |
| 13 | -32.76 | 1087.06 | 33.76 | 32.20 | 127.63 | 436.52 | 308.89 |
| 16 | -26.56 | 1061.25 | 41.67 | 25.47 | 140.52 | 436.97 | 296.45 |
| 19 | -21.18 | 1037.29 | 49.78 | 20.84 | 151.97 | 436.96 | 284.99 |
| 22 | -16.37 | 1014.66 | 58.14 | 17.45 | 162.39 | 436.46 | 274.07 |
| 25 | -12.01 | 993.17 | 66.79 | 14.87 | 171.97 | 435.7 | 263.73 |



Fig. A. 1 Pressure - enthalpy diagram for $\mathrm{CO}_{2}$ (taken from [10]).

This data was further processed into simple polynomials for the purpose of this paper, with results as given in Table A.2, valid for the temperature/pressure ranges as in Table A.1.

Table A.2. Expressions for saturated $\mathrm{CO}_{2}$ liquid and vapour properties versus pressure

| Parameter | Unit | Polynomial as function of | $\mathrm{R}^{2}$ | Equation |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{T}_{\text {sat }}$ | ${ }^{\circ} \mathrm{C}$ | $30.683 \times \ln (\mathrm{p})-111.23$ | 0.9987 | A .1 |
| $\rho_{\mathrm{L}, \text { sat }}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | $-8.172 \times \mathrm{p}+1194.7$ | 0.9967 | A .2 |
| $\rho_{\mathrm{G}, \text { sat }}$ | $\mathrm{kg} / \mathrm{m}^{3}$ | $2.717 \times \mathrm{p}-1.52$ | 0.9996 | A .3 |
| $\rho_{\mathrm{L}, \text { sat } /} / \rho_{\mathrm{G}, \text { sat }}$ | - | $0.1077 \times \mathrm{p}^{2}-5.5726 \times \mathrm{p}+87.342$ | 0.9963 | A .4 |
| $\mathrm{~h}_{\mathrm{L}, \text { sat }}$ | $\mathrm{kJ} / \mathrm{kg}$ | $3.9284 \times \mathrm{p}+75.77$ | 0.9932 | A .5 |
| $\mathrm{~h}_{\mathrm{G}, \text { sat }}$ | $\mathrm{kJ} / \mathrm{kg}$ | $-0.0275 \times \mathrm{p}^{2}+0.9805 \times \mathrm{p}+428.29$ | 0.9832 | A .6 |
| $\mathrm{~h}_{\mathrm{G}, \text { sat }}-\mathrm{h}_{\mathrm{L}, \text { sat }}$ | $\mathrm{kJ} / \mathrm{kg}$ | $-3.9097 \times \mathrm{p}+360.22$ | 0.9973 | A .7 |

## Nomenclature

$A B C$ Ammonium bicarbonate
$A C$ Ammonium carbonate
$B O G$ Boil-off gas
BOR Boil-off rate, \%/day
CAP Chilled ammonia process
CCS Carbon capture and storage
$H$ enthalpy, J
$h$ specific enthalpy, $\mathrm{kJ} / \mathrm{kg}$
$L N G$ Liquefied natural gas
$p$ pressure, Pa or bar
$Q$ heat, J
$\dot{Q}$ heat rate, W or W
$T$ temperature, ${ }^{\circ} \mathrm{C}$ or K
$t$ time, h
$U$ internal energy, J
$W$ work, J
$x$ mass fraction gas (vapour), $\mathrm{kg} / \mathrm{kg}$

## Greek symbols

$\Delta$ difference
$\rho$ density, $\mathrm{kg} / \mathrm{m}^{3}$

## Subscripts and superscripts

$G$ gas (or vapour)
$L$ liquid
sat saturated

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